

Introduction

What is an anomaly?

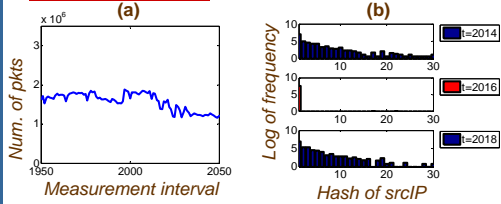


Fig. 1: Fairly stable behavior over time of (a) total number of packets in network, but (b) drastic change in distribution of source IP within a particular flow at $t = 2016$. Data from NYC core router in Abilene backbone network.

- Network anomalies span wide variety of classes/types. Need online and intelligent, anomaly detection method.
- We propose an **online, learning** algorithm, based on the Kernel Recursive Least-Squares (KRLS) algorithm.
- We test on data from Abilene backbone network, and compare with offline, block-based algorithm based on Principal Component Analysis (PCA) [1].

The Architecture

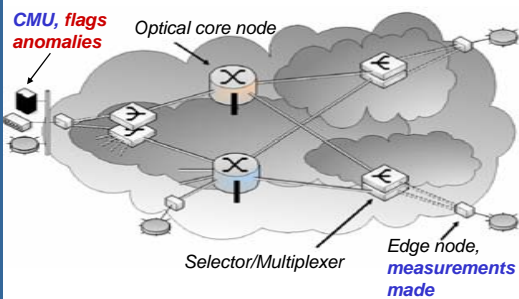


Fig. 2: Traffic statistics collected (in **distributed** manner) at edge nodes, every pre-determined measurement interval. Stats sent to **central monitoring unit (CMU)** which runs **online anomaly detection algorithm, raises alarms**.

- Collect following packet header information at edge nodes: {src edge node, dst edge node, srcIP, dstIP}.
- **Flow** defined as {src edge node, dst edge node} pair.
- \mathbf{x}_t is **Flow Vector**, defined as vector giving number of packets (or bytes) in each flow, normalized, at time t .

The Key Idea

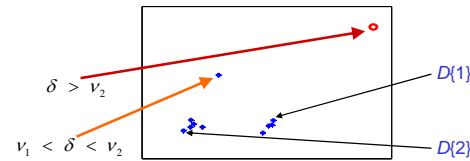


Fig. 3: Simplified depiction of space spanned by 2 sample dictionary elements, $D\{1\}$ and $D\{2\}$. δ is distance metric, v_1 and v_2 are thresholds where $v_1 < v_2$. **Anomaly declared** when $\delta > v_2$, **D expanded** when $v_1 < \delta < v_2$.

Objective: Build a **dictionary** of flow vectors $D = \{\tilde{\mathbf{x}}_j\}_{j=1}^m$, such that mapping onto feature space, $\{\varphi(\tilde{\mathbf{x}}_j)\}_{j=1}^m$, forms an **approximately linearly independent** basis. φ represents mapping from input space to feature space [2].

The Detection Algorithm

• **Initialize** at $t = 1$, by entering \mathbf{x}_1 into dictionary.

• **Iterate** for $t = 2, 3, \dots$

Step 1: New data arrive. Evaluate δ_t , the **degree of linear dependence** of $\varphi(\mathbf{x}_t)$ on the dictionary at time t [2]:

$$\delta_t = \min_{\alpha} \left\| \sum_{j=1}^{m-1} \alpha_j \varphi(\tilde{\mathbf{x}}_j) - \varphi(\mathbf{x}_t) \right\|^2 \quad (1)$$

Step 2: Compare δ_t with thresholds v_1 and v_2 , where $v_1 < v_2$:

- If $\delta_t > v_2$, new input vector is **very** far away, conclude anomaly. Raise **red alarm**, **no change** to dictionary.
- If $v_1 < \delta_t < v_2$, new input vector not sufficiently explained by dictionary. **Add \mathbf{x}_t to dictionary, raise orange alarm**.
- If $\delta_t < v_1$, new input vector falls within normal subspace. **No alarm, no change to dictionary**.

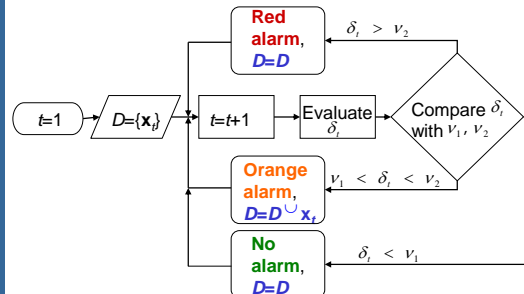


Fig. 4: Outline of online anomaly detection algorithm.

Results

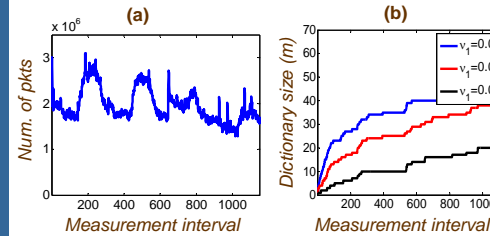


Fig. 5: (a) Variation in total number of packets in network; (b) growth in D for various values of v_1 , with $v_2 = 6v_1$.

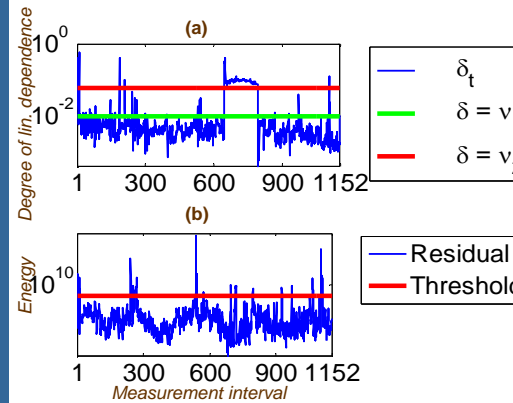


Fig. 6: Comparing (a) δ_t in proposed algorithm with $v_1 = 0.01$ and $v_2 = 6v_1$, with (b) energy in residual subspace using block-based PCA from [1]. Spikes represent anomalies.

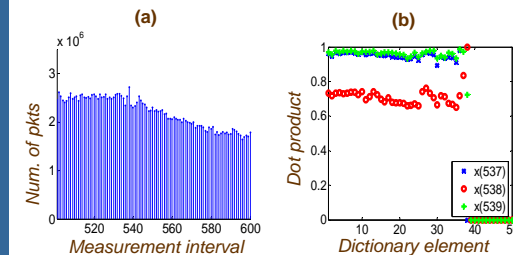


Fig. 7: Example anomaly at $t = 538$. Not easily seen in (a) timeseries of packets, but (b) obvious by observing inner product of \mathbf{x}_t from each dictionary member.

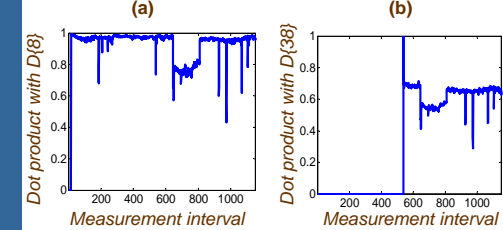


Fig. 8: Progression in time of inner product of \mathbf{x}_t with (a) a normal dictionary member, and (b) an anomalous flow vector that was admitted to dictionary.

Conclusions and Future Work

- Algorithm is **recursive**, there is **no need to relearn** from scratch when new data arrive.
- **Storage requirement and complexity** bounded by $O(m^2)$, i.e. independent of time.
- **Performance comparable to accepted offline, block-based PCA method** in [1].
- Work in progress includes **controlling dictionary** by enabling dropping of obsolete or anomalous elements; confirming anomaly in case of **orange alarm** if relevant \mathbf{x}_t exhibits continually low inner product value to subsequent input vectors.
- Future work involves letting the **data determine the thresholds** v_1 and v_2 .

Acknowledgements

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References

- [1] A. Lakhina, M. Crovella and C. Diot, *Diagnosing Network-Wide Traffic Anomalies*, ACM SIGCOMM, Portland, OR, August 2004.
- [2] Y. Engel, S. Mannor and R. Meir, *The Kernel Recursive Least Squares Algorithm*, IEEE Trans. on Sig. Proc., 52(8), pp.2275--2285, 2004.